


## Research Informed Instructional Considerations for Representing Fractions

The teacher should	It allows students to	References
<ul style="list-style-type: none"> <li>introduce learners to fractions through a context of fair sharing, partitioning with a focus on fairness and number of shares.</li> </ul>	<ul style="list-style-type: none"> <li>construct connection between fractions, multiplication, and division through exploration in context of fair sharing.</li> <li>compare fractional amounts using concrete materials.</li> <li>construct unit fractions and common fractions within a context.</li> <li>avoid the misconception about fractional size that a larger denominator means a larger amount.</li> </ul>	<ul style="list-style-type: none"> <li>Fosnot (2007)</li> <li>Fosnot &amp; Dolk (2002)</li> <li>Van de Walle</li> </ul>
<ul style="list-style-type: none"> <li>engage students in reasoning with repeated halving before creating               <ul style="list-style-type: none"> <li>equal even numbered partitions (e.g., 10)</li> <li>odd numbered partitions (e.g., 7)</li> <li>composition (e.g., 12 can be constructed using a 3x4 array)</li> </ul> </li> </ul>	<ul style="list-style-type: none"> <li>develop an understanding of the representation of fractions first as they can more readily model the mathematics using an appropriate model</li> <li>apply their understanding to increasingly complex partitioning situations.</li> <li>use their multiplicative understanding to partition wholes for denominators which can be factored (composition).</li> </ul>	<ul style="list-style-type: none"> <li>Petit, Laird, Marsden</li> <li>Stiff</li> </ul>
<ul style="list-style-type: none"> <li>use examples and non examples as representations of fractions.</li> </ul>	<ul style="list-style-type: none"> <li>think about what fractions are NOT.</li> <li>surface misconceptions.</li> </ul>	<ul style="list-style-type: none"> <li>Smith</li> <li>Van de Walle</li> </ul>
<ul style="list-style-type: none"> <li>allow students to select their own tools and representations.</li> </ul>	<ul style="list-style-type: none"> <li>share their thinking through the representation, including drawings, and therefore facilitate reasoning. This allows teachers to build upon the students' prior knowledge in meaningful ways.</li> <li>arrive at the conclusion that the parts must be equal in area. Sometimes pre-made partitioned models prevent discovery of such misconceptions.</li> <li>share and refine their understanding of the multiple meanings of fractions, including as parts of a set.</li> <li>think about fraction as part of a whole. Sometimes with pre-partitioned shapes, they rely on counting of partitions instead.</li> <li>construct mental referents which allow them to perform fraction tasks meaningfully. For example, recognize that <math>\frac{1}{4}</math> is less than <math>\frac{1}{2}</math> or that <math>\frac{4}{3}</math> is greater than 1.</li> <li>select manipulatives to model a fraction, which they may find easier to use if they lack the fine motor skills necessary to accurately partition a whole.</li> </ul>	<ul style="list-style-type: none"> <li>Bezuk &amp; Cramer</li> <li>Bruce &amp; Flynn</li> <li>Bruce &amp; Ross</li> <li>Empson &amp; Levi</li> <li>Petit et al</li> <li>Stiff</li> <li>Van de Walle</li> </ul>
<ul style="list-style-type: none"> <li>encourage multiple strategies to explain thinking.</li> </ul>	<ul style="list-style-type: none"> <li>explain their thinking using different strategies, deepening their understanding and use of increasingly precise vocabulary.</li> <li>develop a strong conceptual understanding of the connections between and among representations and strategies, aiding in subsequent learning.</li> <li>make connections to other mathematical concepts, including their knowledge of algebraic relationships.</li> </ul>	<ul style="list-style-type: none"> <li>Bruce &amp; Flynn</li> <li>Empson &amp; Levi</li> <li>Meagher</li> </ul>
<ul style="list-style-type: none"> <li>make precise decisions about the models used and share the rationale with students.</li> </ul>	<ul style="list-style-type: none"> <li>understand that some representations work better in one context than another. The usefulness of a representation is dependent upon the context.</li> </ul>	<ul style="list-style-type: none"> <li>Bruce</li> <li>Petit et al</li> </ul>

## Research Informed Instructional Considerations for Representing Fractions (continued)

The teacher should:	It allows students to:	References
<ul style="list-style-type: none"> <li>incorporate a variety of models and contexts into their instruction</li> </ul>	<ul style="list-style-type: none"> <li>make strong connections between physical models and mathematical concepts.</li> <li>move beyond rote, mechanical manipulations of one manipulative.</li> <li>focus on the important components of fractions (i.e., identify the whole, consider what composes 'equal parts', establish the meaning of the fraction in the given model/context).</li> <li>make connections between different representations, which may uncover inaccurate generalizations or conceptual misunderstandings.</li> </ul>	<ul style="list-style-type: none"> <li>Petit et al</li> </ul>
<ul style="list-style-type: none"> <li>restrict denominators to 12 and less.</li> </ul>	<ul style="list-style-type: none"> <li>work with familiar numbers.</li> <li>easily model the fraction in a variety of ways.</li> </ul>	<ul style="list-style-type: none"> <li>Bezuk &amp; Cramer</li> <li>Van de Walle</li> </ul>
<ul style="list-style-type: none"> <li>engage students in counting by unit fractions (e.g., <math>1/8</math>, <math>2/8</math>, <math>3/8</math>,...).</li> </ul>	<ul style="list-style-type: none"> <li>recognize that the top number counts, while the bottom number tells us what is being counted.</li> <li>consider the part to whole relationship.</li> <li>deepen understanding of a fraction as a single number.</li> </ul>	<ul style="list-style-type: none"> <li>Emperson &amp; Levi</li> <li>Petit et al</li> <li>Van de Walle</li> </ul>
<ul style="list-style-type: none"> <li>monitor understanding of notation and part-whole relationships separately.</li> </ul>	<ul style="list-style-type: none"> <li>investigate the relationships between the fraction concepts and fraction notation.</li> <li>distinguish their level of understanding of each.</li> </ul>	<ul style="list-style-type: none"> <li>Saxe</li> </ul>
<ul style="list-style-type: none"> <li>use models where a region is shaded (without partitions) and ask students to estimate about how much is represented.</li> </ul>	<ul style="list-style-type: none"> <li>develop a sense of what fractions are.</li> <li>think of a fraction as one idea, rather than two numbers.</li> <li>consider the whole region, rather than the individual parts, which minimizes the potential for confusion between whole numbers (the number of parts, the number of shaded parts) and fractions.</li> </ul>	<ul style="list-style-type: none"> <li>Meagher</li> <li>Petit et al</li> <li>Small (2001)</li> <li>Van de Walle</li> </ul>
<ul style="list-style-type: none"> <li>require students to partition an area model to represent a specific fractional value.</li> </ul>	<ul style="list-style-type: none"> <li>refine and/or communicate their understanding of the necessity of congruent pieces for fraction representation.</li> <li>strengthen their understanding of the part-to-whole relationship</li> </ul>	<ul style="list-style-type: none"> <li>Anderson &amp; Wong</li> <li>Petit et al</li> </ul>
<ul style="list-style-type: none"> <li>sequence shading of models so the number of parts in the model equals:               <ul style="list-style-type: none"> <li>the denominator</li> <li>a factor of the denominator</li> <li>a multiple of the denominator</li> </ul>               of the shaded area             </li> </ul>	<ul style="list-style-type: none"> <li>identify the whole unit (and consider how it can change in different contexts).</li> <li>identify the meaning of the equal parts (and consider how they can change in different models).</li> </ul>	<ul style="list-style-type: none"> <li>Petit et al</li> </ul>
<ul style="list-style-type: none"> <li>include different orientations, and also separate the shaded areas, when using area models.</li> </ul>	<ul style="list-style-type: none"> <li>generalize part to whole relationships.</li> </ul>	<ul style="list-style-type: none"> <li>Gould &amp; Outhred</li> <li>Small (2010)</li> </ul>

## Research Informed Instructional Considerations for Representing Fractions (continued)

The teacher should:	It allows students to:	References
<ul style="list-style-type: none"> <li>include models with a perceptual distracter (a visual that does not match the task – e.g., Shade one-third of this circle. )</li> </ul>	<ul style="list-style-type: none"> <li>apply their fraction knowledge.</li> <li>distinguish fractions from whole numbers (i.e., can't just count the correct number of segments).</li> </ul>	<ul style="list-style-type: none"> <li>Case &amp; Moss</li> <li>Petit et al</li> </ul>
<ul style="list-style-type: none"> <li>have students break fractions into parts (e.g., <math>5/4 = 1/4 + 4/4</math> or <math>3/4 + 1/2</math>, etc)</li> </ul>	<ul style="list-style-type: none"> <li>increase flexibility with number.</li> <li>compose and decompose fractions to make them friendly.</li> <li>view a fraction as a single numeric value.</li> </ul>	<ul style="list-style-type: none"> <li>Empson &amp; Levi</li> <li>Fosnot &amp; Dolk (2002)</li> <li>Petit et al</li> <li>Van de Walle</li> </ul>
<ul style="list-style-type: none"> <li>engage students in activities which extend their concept of unit (e.g., if the yellow trapezoidal pattern block is a whole, then what is the value of a green triangle? Also, if this area represents <math>3/5</math>, draw the whole.)</li> </ul>	<ul style="list-style-type: none"> <li>develop flexibility of unit.</li> <li>reinforce their concept of unit.</li> <li>deepen understanding of equivalence and relative size.</li> </ul>	<ul style="list-style-type: none"> <li>Bezuk &amp; Cramer</li> <li>Petit et al</li> <li>Van de Walle</li> </ul>
<ul style="list-style-type: none"> <li>ask students to represent fractions using a variety of number lines</li> </ul>	<ul style="list-style-type: none"> <li>consolidate their understanding of fraction as number (although they may first revert to whole number reasoning).</li> <li>connect fractions to their understanding of measurement.</li> <li>apply proportional reasoning to the location of fractions on a number line.</li> <li>connect the area representation to the number line by possibly constructing area models underneath and aligned with the number line.</li> </ul>	<ul style="list-style-type: none"> <li>Petit et al</li> </ul>